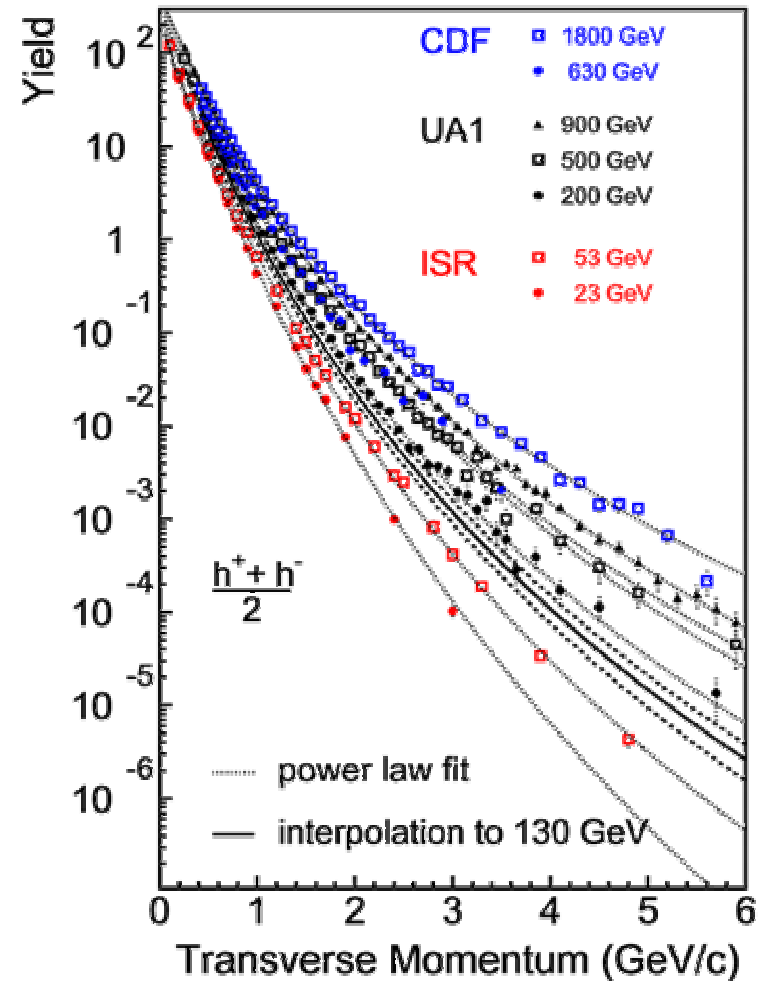
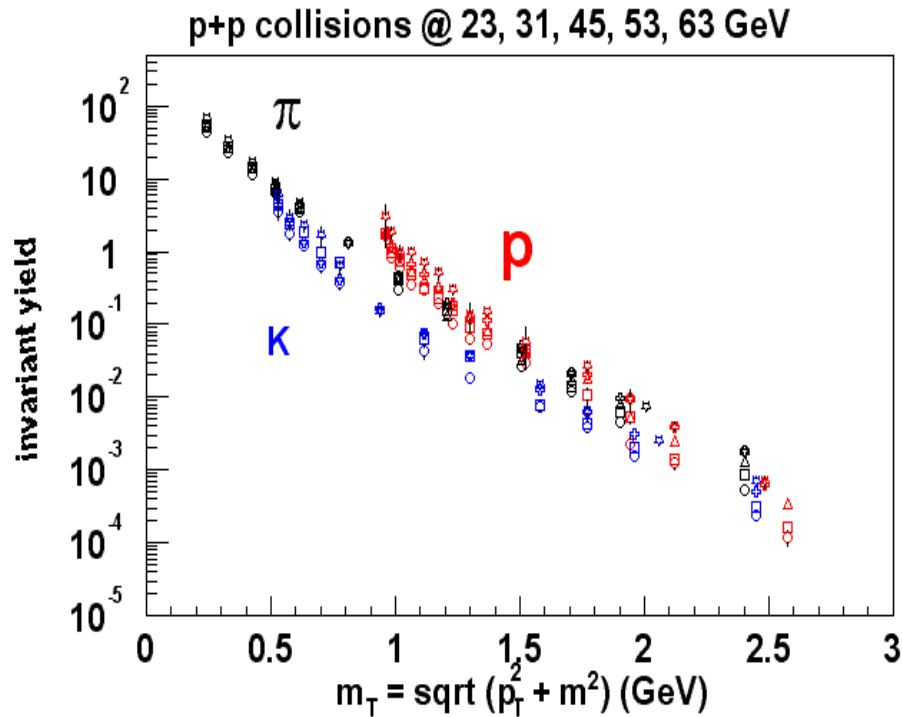


Spectral shapes in pp collisions

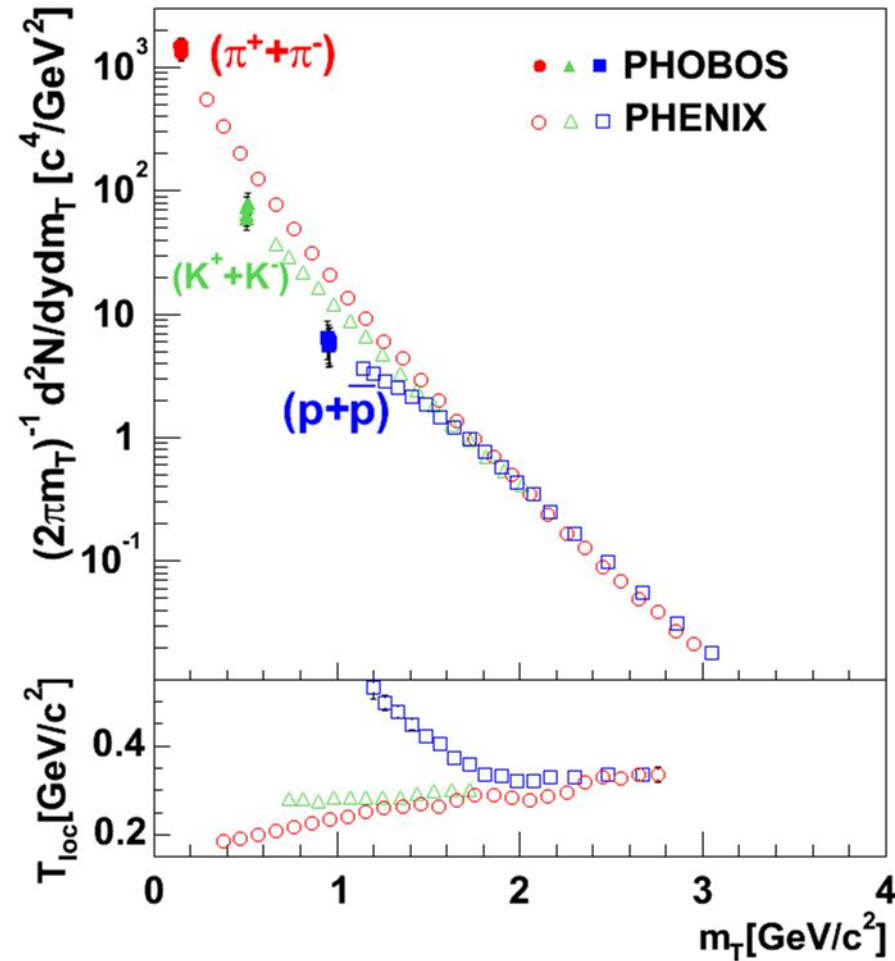
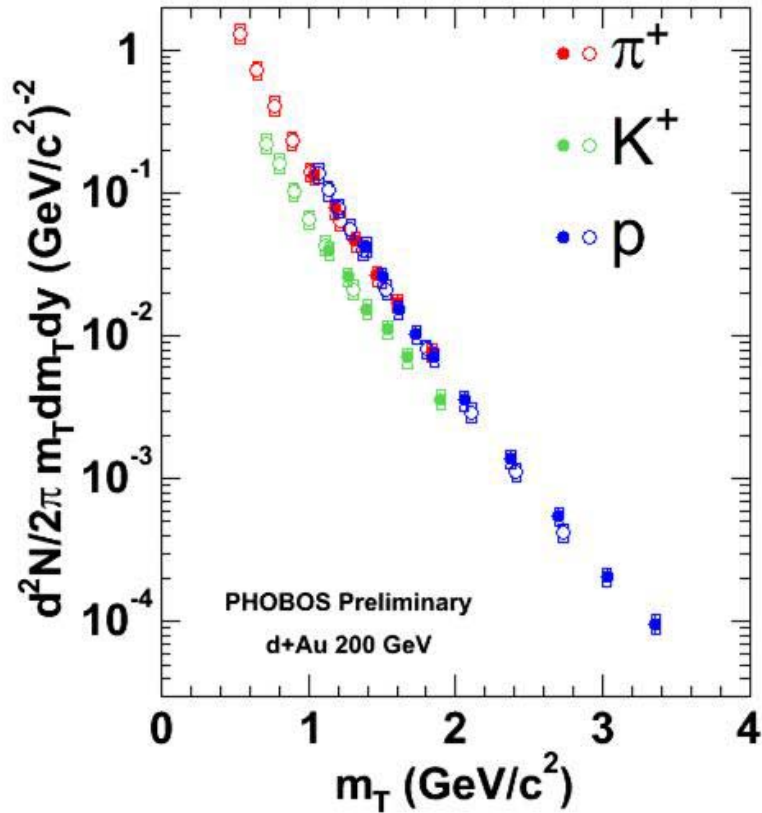


Mt-scaling for soft particles

Power-law tail from hard scattering
Increasing with energy



Scaling of spectra in dA and AA collisions



- m_T scaling in pp and dA, but NOT in AA. Signature of radial flow.



Source is assumed to be:

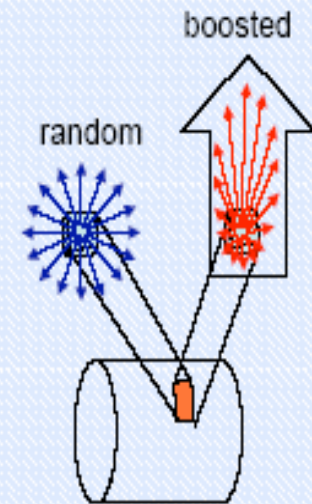
- Locally thermal equilibrated
- Boosted in radial direction

E.Schnedermann, J.Sollfrank, and U.Heinz, Phys. Rev. C48, 2462(1993)

$$E \frac{d^3 N}{dp^3} \propto \int_{\sigma} e^{-(u^{\mu} p_{\mu})/T_{fo}} p d\sigma_{\mu} \Rightarrow$$

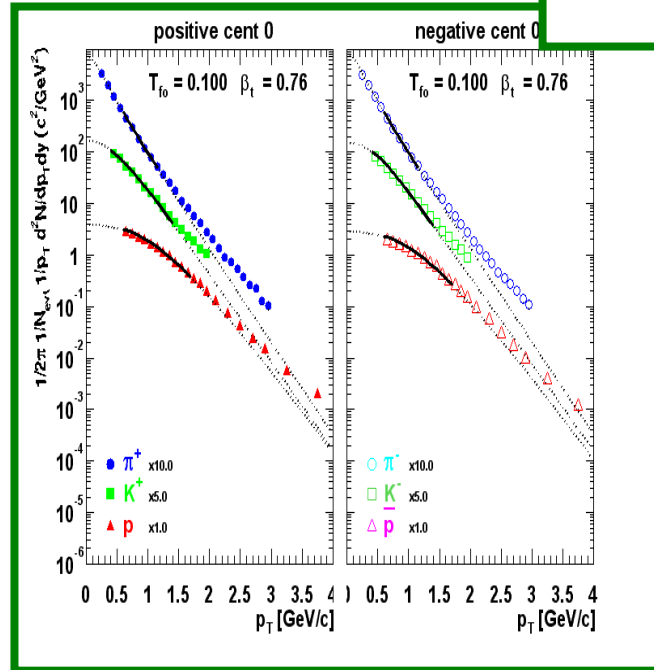
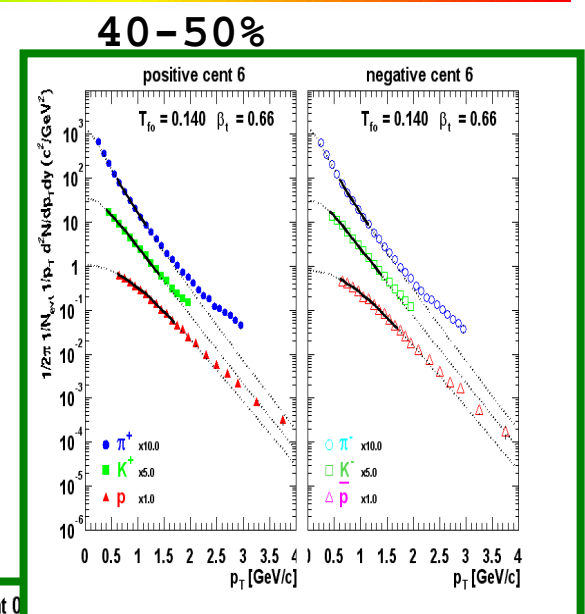
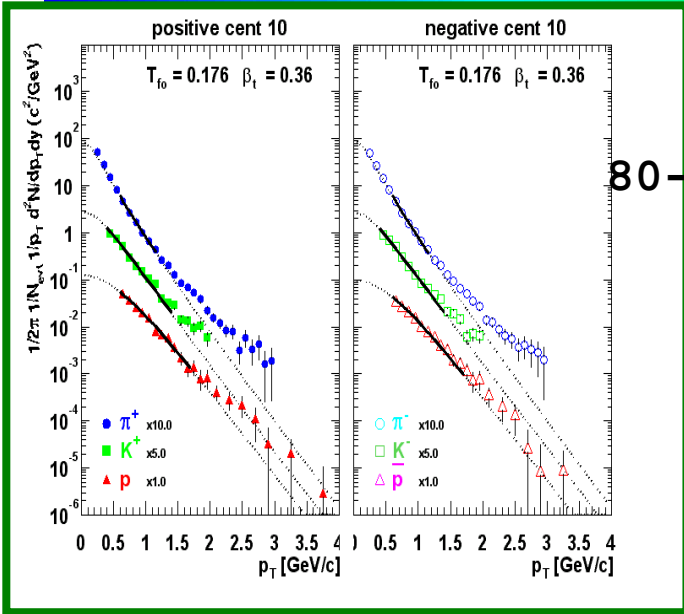
$$\frac{dN}{m_T dm_T} \propto \int_0^R r dr m_T K_1 \left(\frac{m_T \cosh \rho}{T_{fo}} \right) I_0 \left(\frac{p_T \sinh \rho}{T_{fo}} \right)$$

$$\rho = \tanh^{-1} \beta_T \quad \beta_T = \beta_s \left(\frac{r}{R} \right)^{\alpha} \quad \alpha = 0.5, 1, 2$$

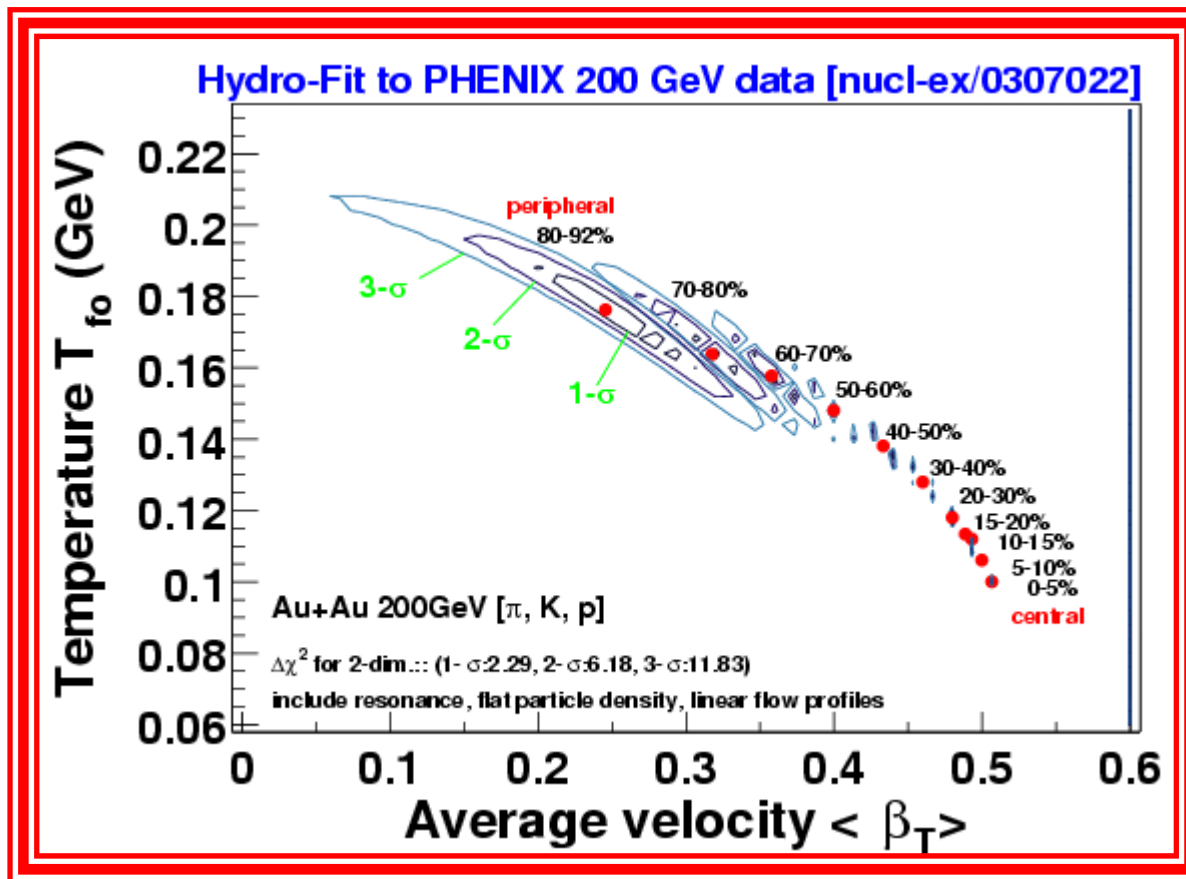


Extract thermal temperature T_{fo} and velocity parameter $\langle \beta_T \rangle$

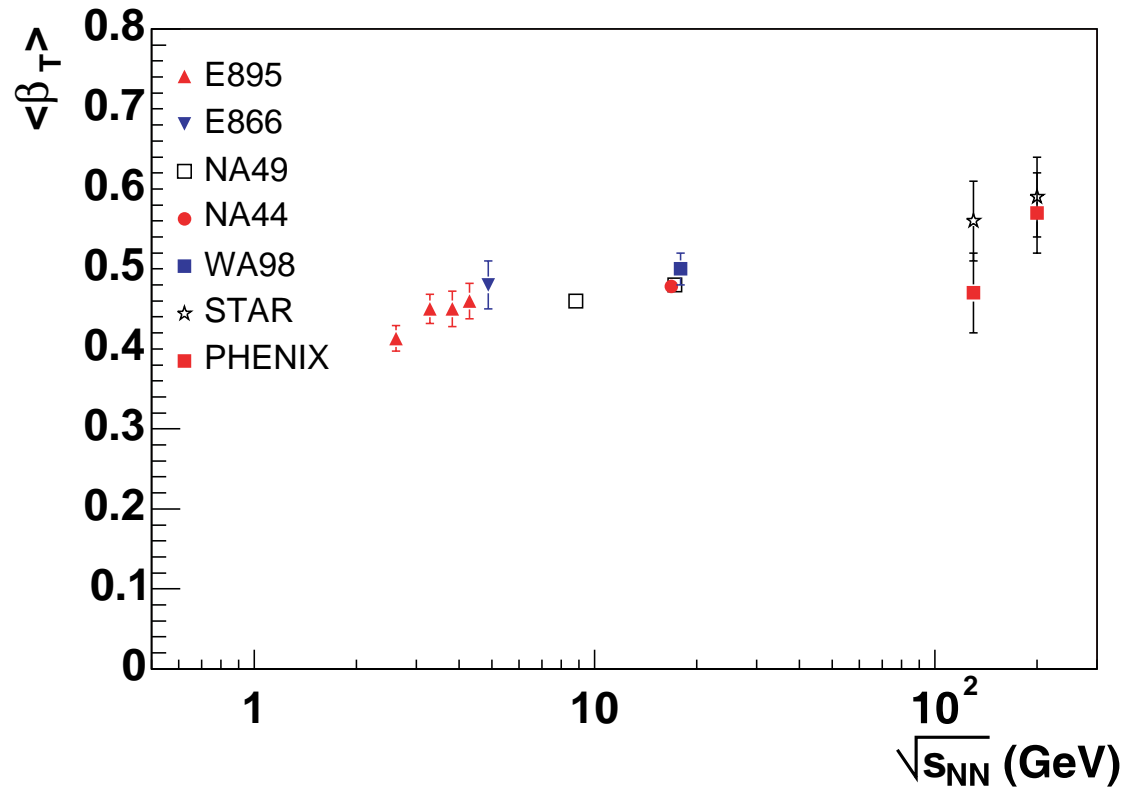
Fitting π, K, p with hydrodynamics model



Blast wave fits: T_{fo} and flow velocity



Flow velocity vs energy



$\langle \beta_T \rangle$ slowly increasing from AGS to SPS to RHIC



Basics of Hydrodynamics

Hydrodynamic Equations

$$\partial_\mu T^{\mu\nu} = 0, \quad \text{Energy-momentum conservation}$$

$$\partial_\mu n_i^\mu = 0 \quad \text{Charge conservations (baryon, strangeness, etc...)}$$

For perfect fluids (neglecting viscosity),

$$T^{\mu\nu} = (e + P)u^\mu u^\nu - P g^{\mu\nu}$$

Energy density

Pressure

4-velocity

Need **equation of state**
(EoS)

$$P(e, n_B)$$

to close the system of eqs.
→ Hydro can be connected
directly with **lattice QCD**

Within ideal hydrodynamics, pressure gradient dP/dx is the driving force of collective flow.

→ Collective flow is believed to reflect information about EoS!

→ Phenomenon which connects 1st principle with experiment

Caveat: Thermalization, $\lambda \ll$ (typical system size)

Inputs to Hydrodynamics

